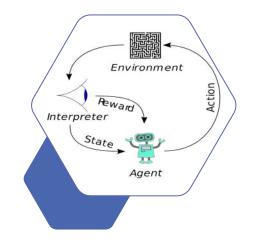
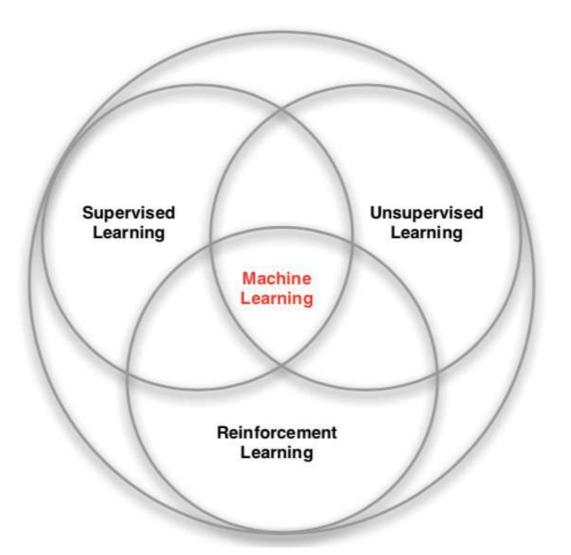


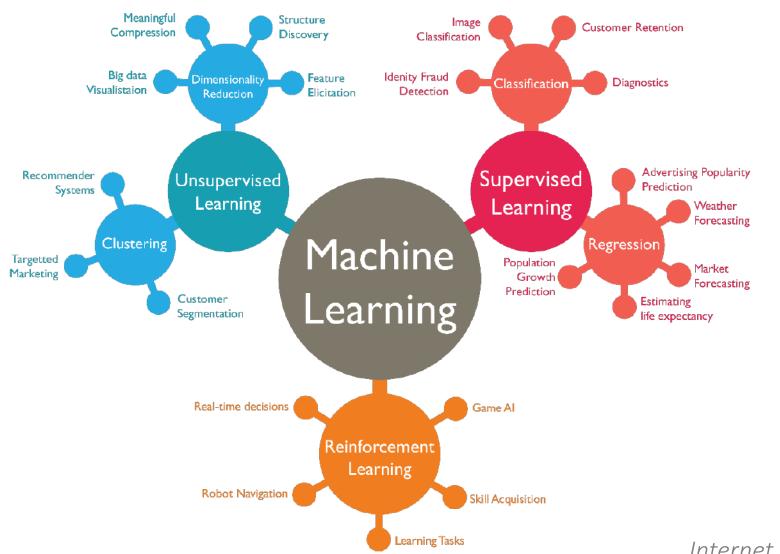
Branches of Machine Learning

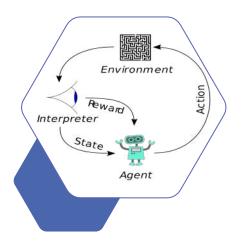






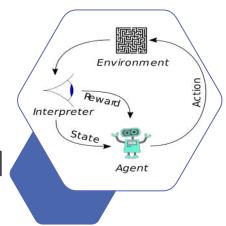
Branches of Machine Learning



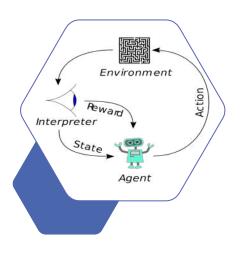


Branches of Machine Learning

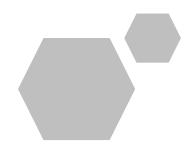
Supervised learning: Learning from a training set of labeled data provided by a knowledgable external supervisor.



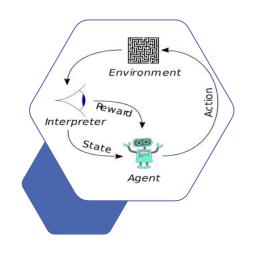
- Unsupervised learning: Learning the inherent structure of data without the use of explicitly-provided labels.
- Reinforcement learning: Learning what to do—how to map situations to actions—so as to maximize a numerical reward signal (closed-loop problem).



Reinforcement Learning (RL)



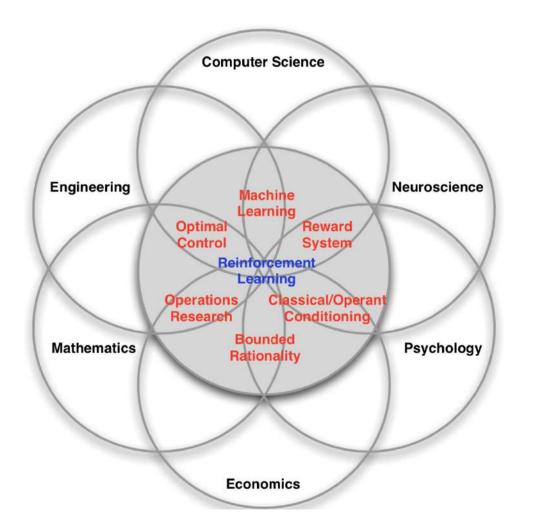
Machine vs. Reinforcement Learning

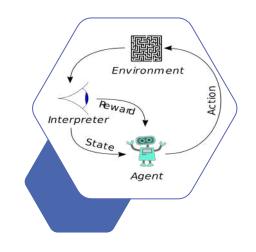


- More focused on goal-directed learning from interaction
- There is no supervisor, only a reward signal
- No instantaneous feedback (delayed)
- Time really matters (sequential, non i.i.d. data)
- Agent's actions affect the subsequent data it receives.



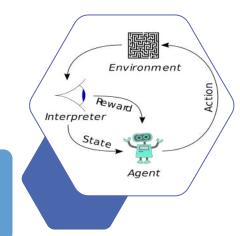
Many faces of RL







Historical Background





Original motivation: animal learning



Early emphasis: neural net implementations and heuristic properties



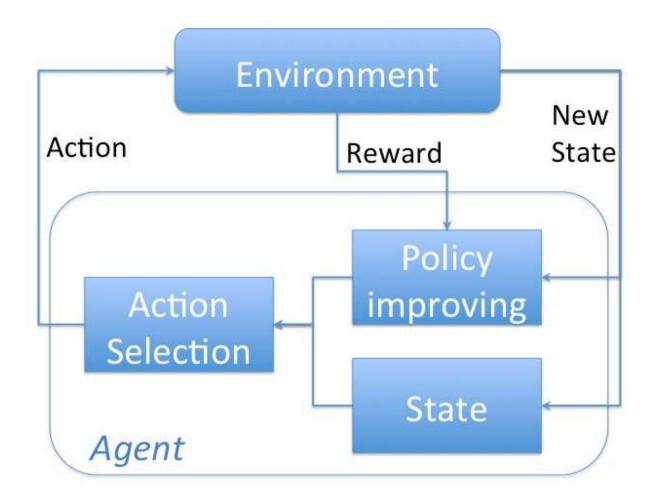
Operations research, optimal control theory, dynamic programming, Al state-space research

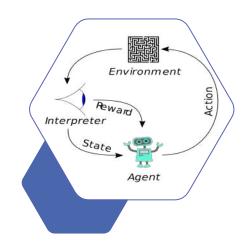


Best formalized as a set of techniques to handle: MDPs or P(artially)O(bservable)MDPs



RL Task

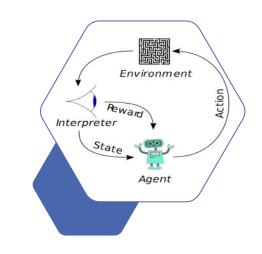






RL Task

$$\begin{array}{c}
a(1) & a(2) & a(3) \\
s(0) \xrightarrow{r(1)} s(1) \xrightarrow{r(2)} s(2) \xrightarrow{r(3)} s(3) \dots
\end{array}$$

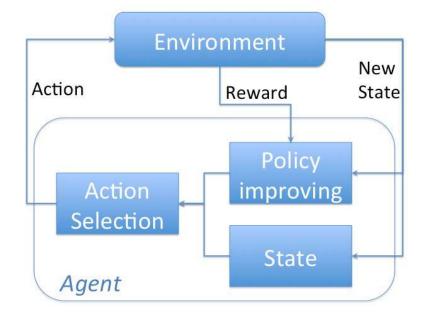


Goal: learn to choose actions that maximize the cumulative reward

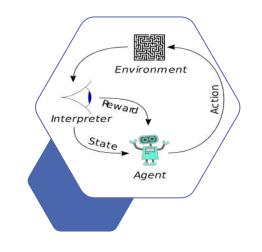
$$r(0) + \gamma r(1) + \gamma r(2) + \gamma r(3) + \dots$$



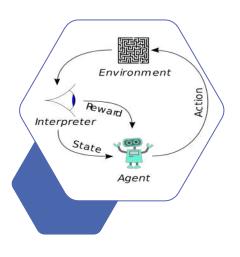
where $0 \le \gamma < 1$



Elements of an RL agent



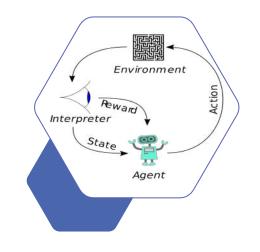
- Policy: Defines the agent's way of behaving
- Reward signal: Defines the goal of the RL problem; Agent's objective is to maximize the total reward in the long run
- Value function: Specifies what is good in the long run
- Model: Mimics the behavior of the environment.



Markov Decision Processes (MDP)



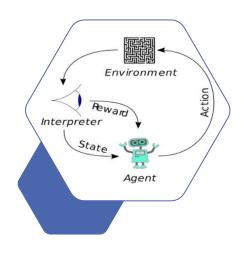
Introduction to MDPs



- MDPs formally describes a framework for RL.
- The environment is fully observable, i.e., the current state completely characterizes the process.
- Almost all RL problems can be formalized as MDPs.



Markov Decision Processes



- Finite set of states S
- Finite set of actions A(s), $s \in S$
- Immediate reward function

$$R: S \times A \rightarrow R$$

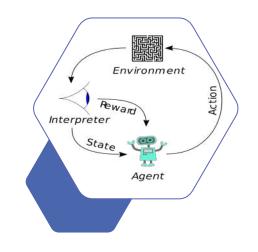
Transition (next-state) function

$$T: S \times A \rightarrow S$$

- More generally, R and T are treated as stochastic
- Our focus: discrete time MDPs.



Markov Decision Processes



Markov Property for MDPs

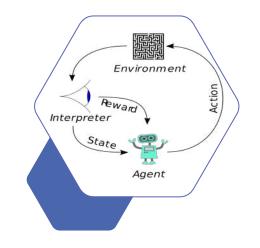
$$P(s' \mid s, a)$$

 $s', s \in S, \quad a \in A(s)$

Next state is a function of current <u>state</u> and the <u>action taken!</u>



Markov Decision Processes



• If no rewards and only one action, this is just a Markov chain(or Controlled Markov Chain)

Overall objective is to determine a policy

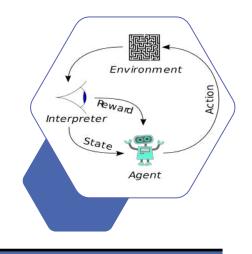
$$\pi: S \to A$$

such that some measure of cumulative reward is optimized



E.g,
$$r(0) + \gamma r(1) + \gamma r(2) + \gamma r(3) + ...$$

What is a policy?

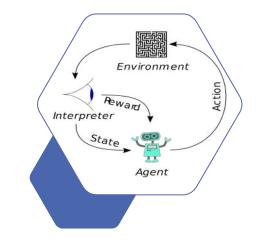


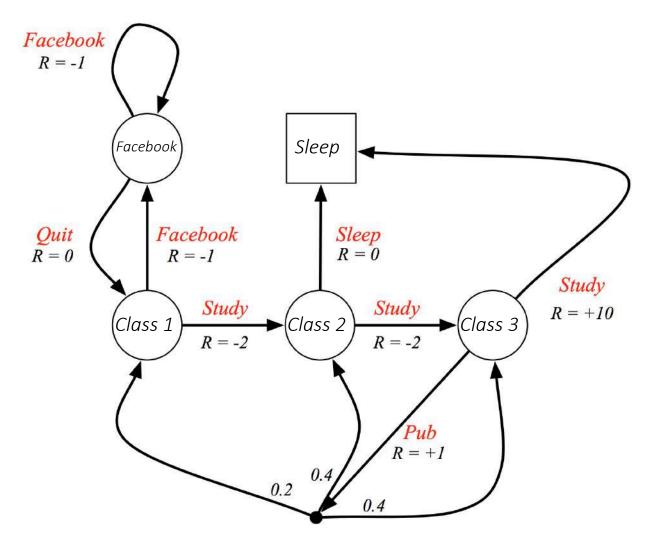
- A **policy** is the agent's behavior
- It is a map from state to action.

If agent is in state	Then a good action is
s ₁	a ₃
s_2	a ₇
s ₃	a ₁
S ₄	a_3
ree	***



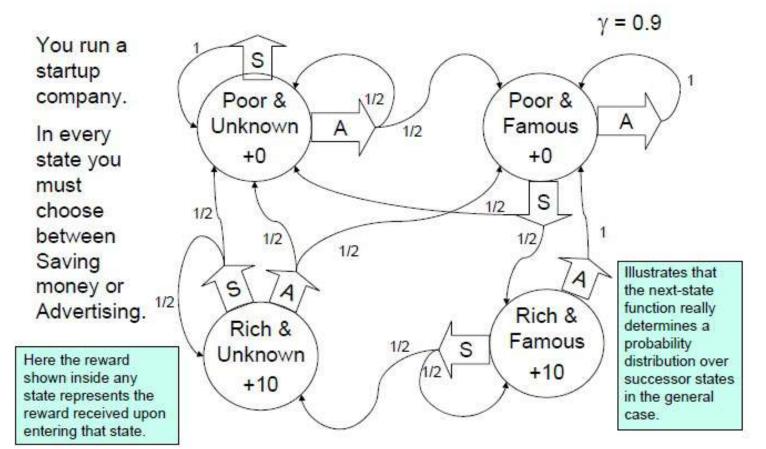
Student Markov Decision Process

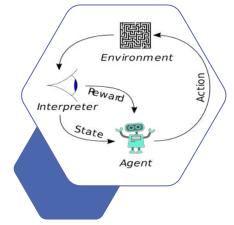




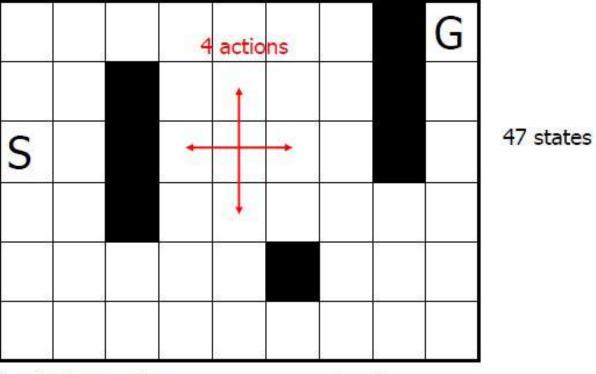


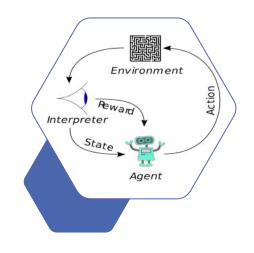
A Markov Decision Process

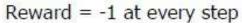




Another MDP







 $\gamma = 1$

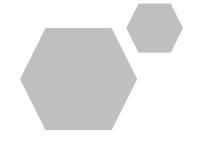
G is an absorbing state, terminating any single trial, with a reward of 100

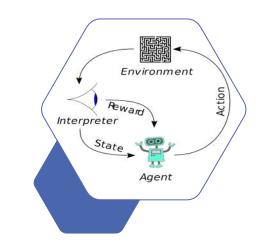
Effect of actions is deterministic



Applications of MDPs

- Many important problems are MDPs
 - Robot path planning
 - Travel route planning
 - Elevator scheduling
 - Autonomous aircraft navigation
 - Manufacturing processes
 - Network switching & routing
 - •





 Many of these have been successfully handled using RL methods.

Brief Summary of Concepts

Environment

Reward
Interpreter

State

Agent

- The agent and its environment interact over a sequence of discrete time steps
- The specification of their interface defines a particular task:
 - the actions are the choices made by the agent
 - the *states* are the basis for making the choices
 - the *rewards* are the basis for evaluating the choices
- A policy is a stochastic rule by which the agent selects actions as a function of states
 - The agent's objective is to maximize the amount of reward it receives over time.

Value Function



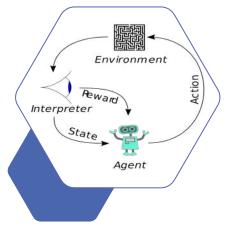
$$V^{\pi}(s) = \sum_{t=0}^{\infty} \gamma^t r(t),$$

where s(0) = s



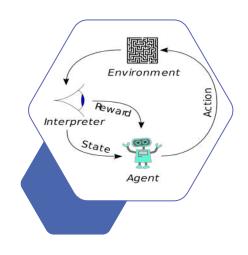
- Each subsequent s(t+1) arises from the transition function T
- Each immediate reward r(t) is determined by the immediate reward function R
- γ is a given discount factor in [0, 1]

Reminder: Use expected values in the stochastic case.



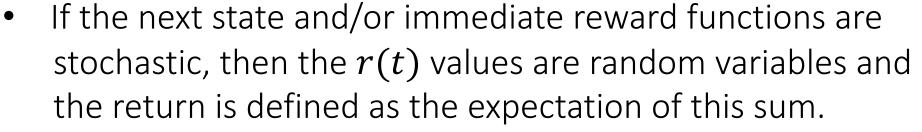
Discount factor γ

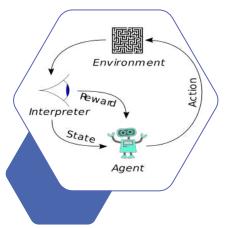
Models idea: Future rewards are not worth as much as immediate rewards



- Used in economic models
- Uncertainty about the future
- Models situations where there is a nonzero fixed probability $1-\gamma$ of termination at any time
- Tradeoff between myopic ($\gamma=0$) vs. foresighted optimization (γ close to 1)
- ...and makes the math work out nicely with bounded rewards, sum guaranteed to be finite even in infinite-horizon case.

Technical Remarks





- If the MDP has absorbing states, the sum may actually be finite
 - In that case $\gamma = 1$ is allowed, i.e., no discount
 - We stick with this infinite sum notation for the sake of generality
 - The formulation we use is called infinite-horizon.



Optimal Policies

• Objective: Find a policy π^* such that

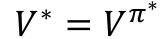
$$V^{\pi^*}(s) \ge V^{\pi}(s)$$

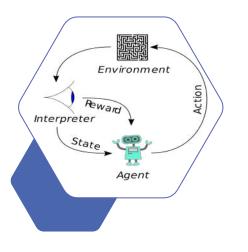
for any policy π and any state s

Such a policy is called an optimal policy

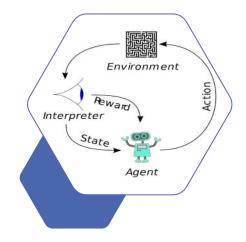








Interesting Facts



- For every MDP such that S is discrete and A(s) is finite there exists an optimal policy
 - This theorem can be easily extended to the case in which A(s) is a *compact* set.
- It is a policy such that for every possible start state there is no better option than to follow the policy.

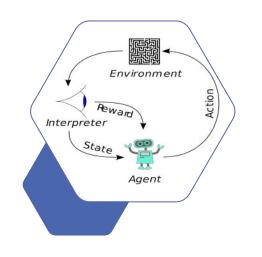


Finding an Optimal Policy

- Idea:
 - 1. Run through all possible policies.
 - 2. Select the best.

What's the problem ??





Finding an Optimal Policy

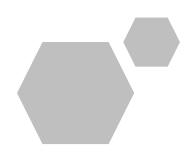
- Environment

 Reward

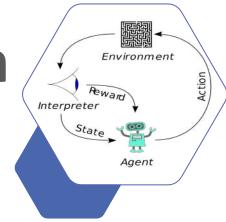
 Interpreter

 State

 Agent
- Dynamic Programming approach: Determine the optimal value function for each state Select actions according to this optimal value function V^*
- How do we compute V^* ?
 - Magic words: Bellman equation(s)



Derivation of the Bellman Equation



• Given the state transition $s \rightarrow s'$

$$V^{\pi}(s) = \sum_{t=0}^{\infty} \gamma^{t} r(t)$$

$$= r(0) + \gamma \sum_{t=0}^{\infty} \gamma^{t} r(t+1)$$

$$= r(0) + \gamma V^{\pi}(s')$$



Bellman Equations

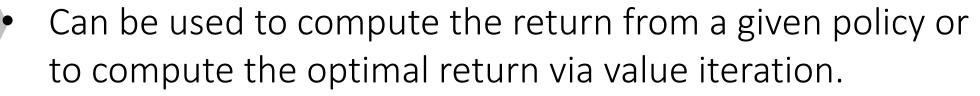
• For any state s and policy π

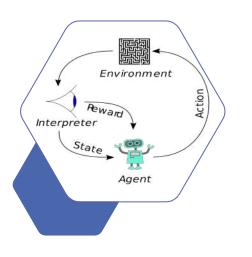
$$V^{\pi}(s) = R(s, \pi(s)) + \gamma V^{\pi}(T(s, \pi(s)))$$



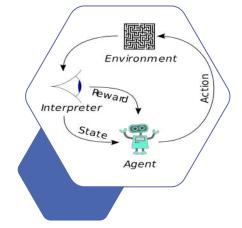
$$V^{*}(s) = \max_{a} \{ R(s, a) + \gamma V^{*}(T(s, a)) \}$$

Recurrence relations





Bellman Equations: General Form



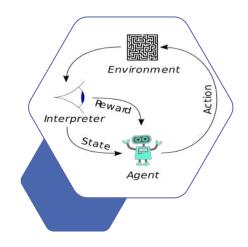
 For completeness, here are the Bellman equations for stochastic and discrete time MDPs:

$$V^{\pi}(s) = R(s, \pi(s)) + \gamma \sum_{s'} P_{ss'}(\pi(s)) V^{\pi}(s')$$

$$V^{*}(s) = \max_{a} \{ R(s, a) + \gamma \sum_{s'} P_{ss'}(a) V^{*}(s') \}$$

where R(s,a) now represents $E(R \mid s,a)$ and $P_{ss'}(a)$ is the probability that the next state is s' given that action a is taken in state s

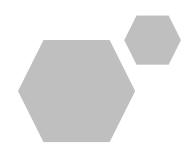
From Values to Policies



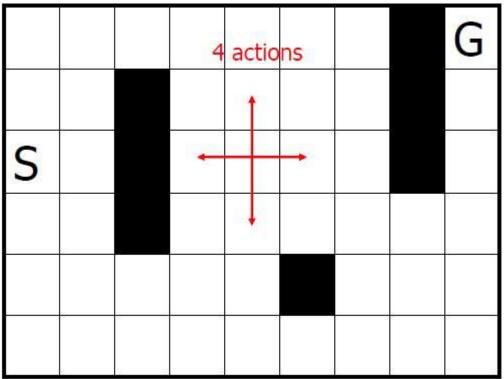
• Given the optimal value function V^* it follows from Bellman equation that the optimal policy can be computed as:

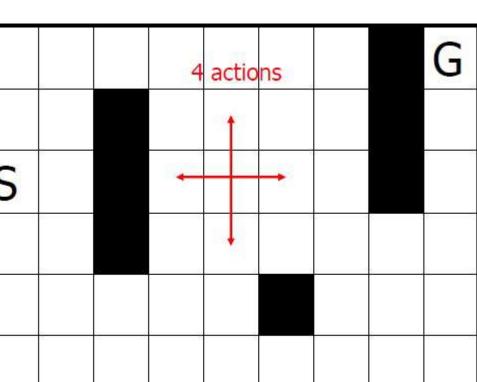
$$\pi(s) = \underset{a}{\operatorname{argmax}} \{R(s, a) + \gamma V^*(s')\}$$

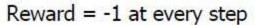
• An optimal policy is said to be greedy for V^*



An example: Maze task



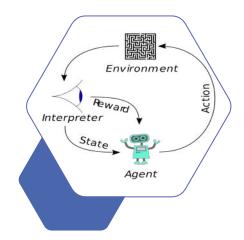




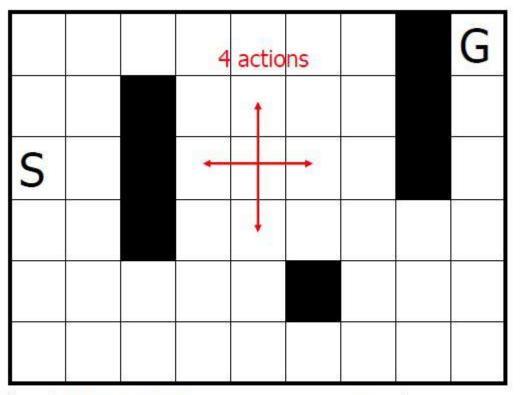
$$\gamma = 1$$

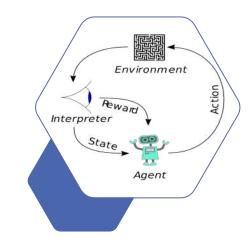
G is an absorbing state, terminating any single trial, with a reward of 100

Effect of actions is deterministic

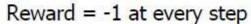


An example: Maze task





How would you model the MDP?



$$\gamma = 1$$

G is an absorbing state, terminating any single trial, with a reward of 100

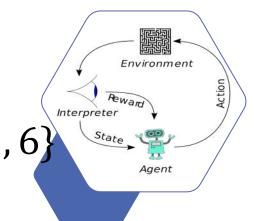
Effect of actions is deterministic



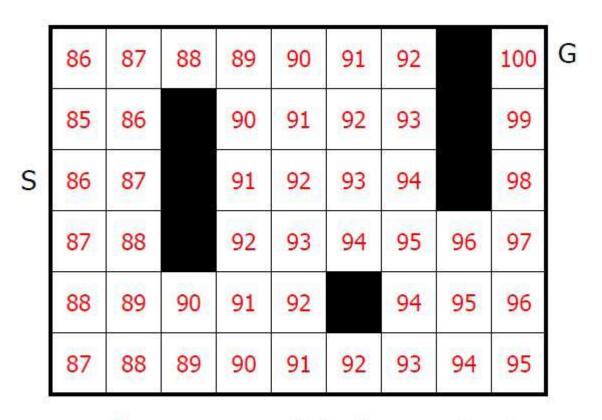
Maze task: MDP Model

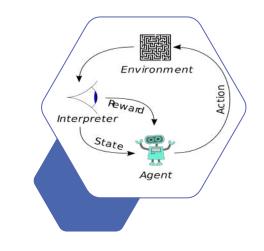
- State is a pair: $s = (x, y), x \in \{1, ..., 9\}$ and $y \in \{1, ..., 6\}$ defining the robot's position.
- Actions: $A(s) = \{\text{up, down, left, right}\}\$ (except for those states near the black squares)
- Reward Function: $R(s) = \begin{cases} -1, & \forall s \neq G \\ 100, & \text{if } s = G \end{cases}$

• Transition function: $s' = \begin{cases} (x+1,y) & \text{if } a = \text{right} \\ (x-1,y) & \text{if } a = \text{left} \\ (x,y+1) & \text{if } a = \text{up} \\ (x,y-1) & \text{if } a = \text{down} \end{cases}$



Maze task: Value Function





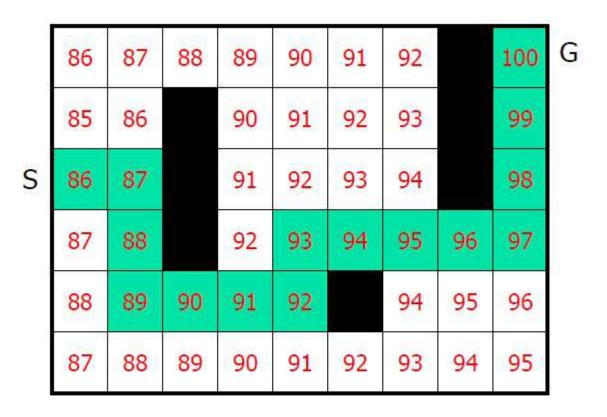


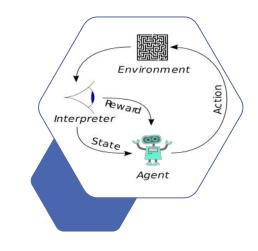
What's an optimal path from S to G?



38

Maze task: Optimal Path







Why On-line learning is important?

Environment

Reward

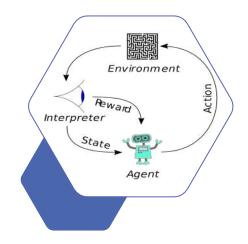
Interpreter

State

Agent

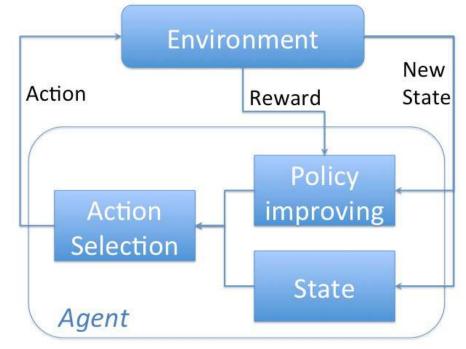
- Assumption: All system parameters to be known.
- Finding the optimal policy becomes a straightforward computational problem
 - E.g., value iteration, but even policy iteration, linear programming, etc...
- What if rewards/transitions probabilities are unknown? Can we compute the optimal policy?

Agent-Environment Interaction



 Everything inside the agent is completely known and controllable by the agent.

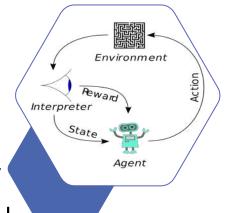
 Everything outside is incompletely controllable but may or may not be completely known.





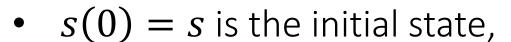
Agent Knowledge

- A reinforcement learning problem can be posed in a variety
 of different ways depending on assumptions about the level
 of knowledge initially available to the agent.
- In problems of *complete knowledge*, the agent has a complete and accurate model of the environment's dynamics.
- If the environment is an MDP, then such a model consists of the one-step transition probabilities and expected rewards for all states and their allowable actions.
 - In problems of <u>incomplete knowledge</u>, a complete and perfect model of the environment is not available.

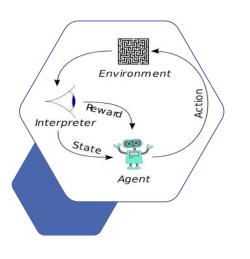


• For any policy π , define $Q^{\pi}: S \times A \to R$ by

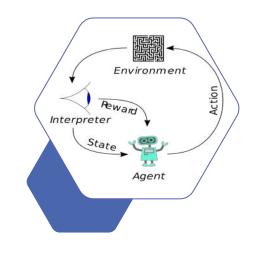
$$Q^{\pi}(s,a) = \sum_{t=0}^{\infty} \gamma^t r(t)$$



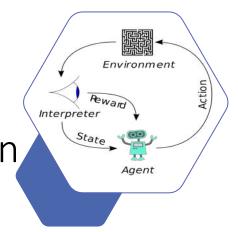
- a(0) = a is the action taken,
- ullet all subsequent states, actions, and rewards arise following policy π
- Just like V^{π} except that action a is taken at the very first step and only after this, policy π is followed Bellman equations can be rewritten in terms of Q-values.



If agent is in state	An starts with this action and then follows the policy	Return should be
s_1	a_1	-5
s_1	a_2	3
s ₂	a_1	17.1
S ₂	a_2	10
•••	•••	•••



• Relationship between Value function and Q-function (given the state transition $s \rightarrow s'$)



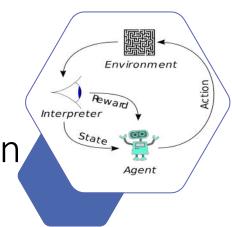
$$V^{\pi}(s) = R(s, \pi(s)) + \gamma V^{\pi}(s')$$

VS.

$$Q^{\pi}(s,a) = R(s,a) + \gamma V^{\pi}(s')$$



• Relationship between Value function and Q-function (given the state transition $s \to s'$)



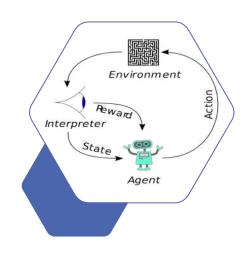
$$V^{\pi}(s) = R(s, \pi(s)) + \gamma V^{\pi}(s')$$

VS.

$$Q^{\pi}(s,a) = R(s,a) + \gamma V^{\pi}(s')$$



• Define $Q^* = Q^{\pi^*}$, where π^* is an optimal policy



$$Q^*(s,a) = R(s,a) + \gamma V^*(s')$$

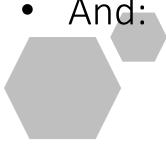
Since:

$$V^{*}(s) = \max_{a} \{ R(s, a) + \gamma V^{*}(s') \}$$

Then:

$$V^*(s) = \max_a Q^*(s, a)$$

And:

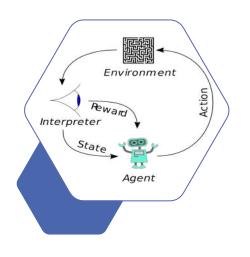


$$Q^*(s, a) = R(s, a) + \gamma \max_{a'} Q^*(s', a')$$

• The optimal policy π^* is greedy for Q^* , that is



[it follows from
$$V^*(s) = \max_a Q^*(s, a)$$
]





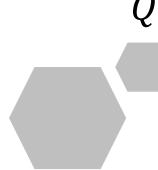
Environment

Q-learning Algorithm

- Q is the estimated utility function
 - It tells us how good an action is, given a certain state



- It allows to compute the optimal policy.
- Q-learning is based on an online estimation of the Q function $Q(s,a) \leftarrow (1-\alpha)Q(s,a) + \alpha \left[r(s,a) + \gamma \max_{a'} Q(s',a')\right]$



Q-learning Algorithm

Initialize Q(s, a) arbitrarily

Repeat (for each decision epoch)

Initialize s

Repeat (for each step of episode)

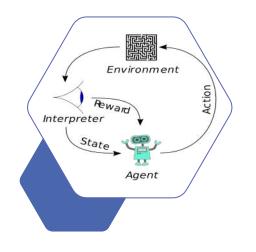
Choose a from s using a policy derived from Q

Take action a, observe r(s, a),

$$Q(s,a) \leftarrow (1-\alpha)Q(s,a) + \alpha \left[r(s,a) + \gamma \max_{a'} Q(s',a') \right]$$

$$s \leftarrow s'$$

until s is terminal



Environment

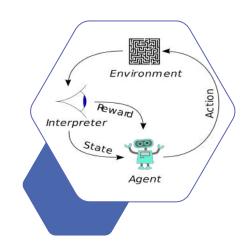
Exploitation and Exploration

- Q-learning algorithm does not specify what the agent should actually do. The agent learns a Q-function that can be used to determine an optimal action.
- There are two things that are useful for the agent to do:
 - exploit the knowledge that it has found at the current state s by taking one of the actions a that maximizes Q[s,a].
 - explore in order to build a better estimate of the optimal Q-function. That is, it should select a different action from the one that it currently thinks is best.

Exploitation and Exploration

Choose a from s using a policy derived from Q

- Simple Approach: ε-greedy policy
 - $-\epsilon$ small number, e.g., 0.1



Generate a random number p

if $p \le \varepsilon$

Choose an action at random \rightarrow explore

else

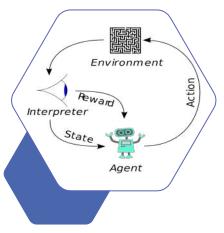
Choose the greedy action

$$a^* = \arg\max_a Q(s, a) \to \text{exploit}$$

end

Q-learning Discussion

• Q-learning is guaranteed to converge to the optimal Q-values if all Q(s,a) values are updated infinitely often (Watkins and Dayan 1992).

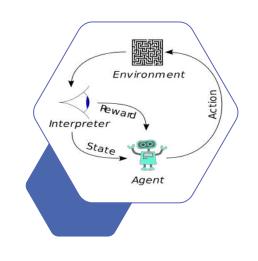


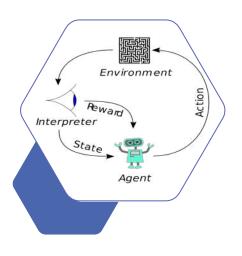
- It follows that exploration is necessary
 - A common approach is the ε-greedy strategy
- Q-learning can be very slow to converge to the optimal policy, especially if the state space is large.
- One of the biggest challenges in the RL field is to *speed up* the learning process.

Learning or Planning?

- Classical DP emphasis for optimal control
 - Dynamics and reward structure known
 - Off-line computation
- Traditional RL emphasis
 - Dynamics and/or reward structure initially unknown
 - On-line learning

• Computation of an optimal policy off-line with known dynamics and reward structure can be regarded as planning.

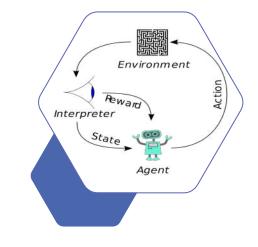


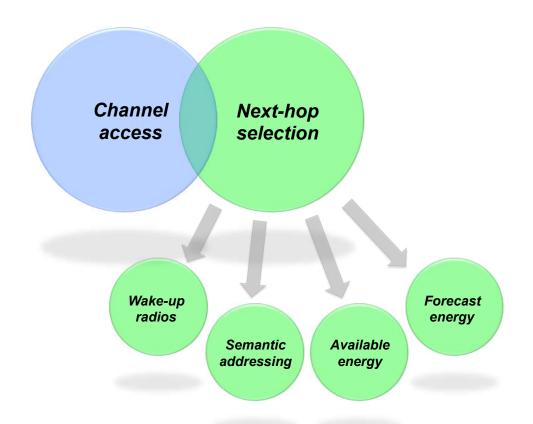


Reinforcement Learning in Practice



The WHARP forwarding strategy





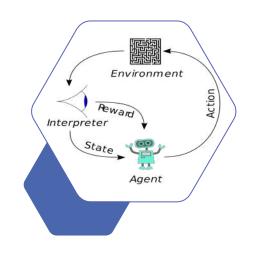


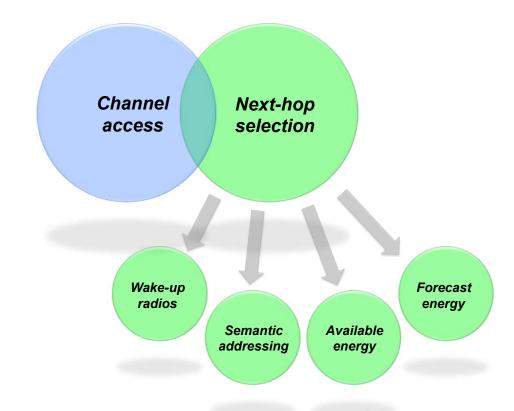
S. Basagni, V. Di Valerio, G. Koutsandria, C. Petrioli, and D. Spenza. "WHARP: A wake-up radio and harvesting-based forwarding strategy for green wireless networks," in *Proceedings of IEEE MASS* 2017, Orlando, FL, USA, October 22–25 2017.

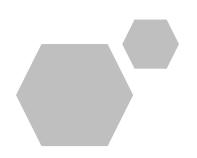
Internet of Things A.Y. 20-21

The WHARP forwarding strategy

 Objective: Optimize energy consumption through a «smart» selection of next-hop relays.

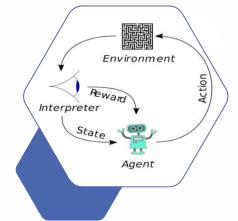






The WHARP forwarding strategy

Semantic awakenings: Distance from the sink



- Nodes decide whether to participate to the relay selection process based on a proactive Markov Decision Process mechanism
 - 1. Available energy
 - 2. Forecast energy
- MDP solution method: Backward Value Iteration (BVI)
 - WHARP decisions optimize system performance over time
 - S. Basagni, V. Di Valerio, G. Koutsandria, C. Petrioli, and D. Spenza. "WHARP: A wake-up radio and harvesting-based forwarding strategy for green wireless networks," in *Proceedings of IEEE MASS* 2017, Orlando, FL, USA, October 22–25 2017.

 Internet of Things A.Y. 20-21

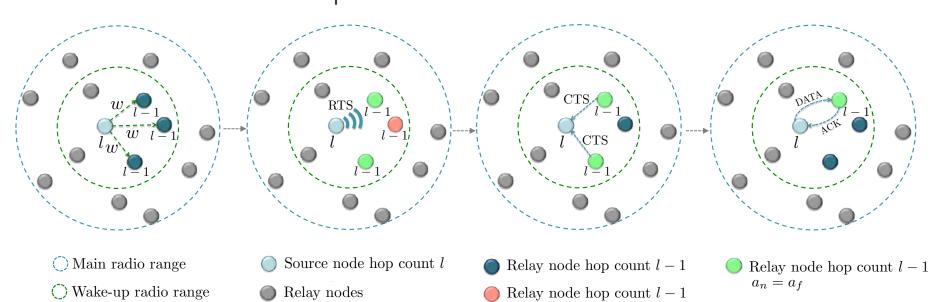
Environment

Agent

Interpreter

The WHARP forwarding strategy

- The MDP policy outputs either green or red.
- Green output: Nodes turn on their main radio
- Red output: Nodes remain asleep



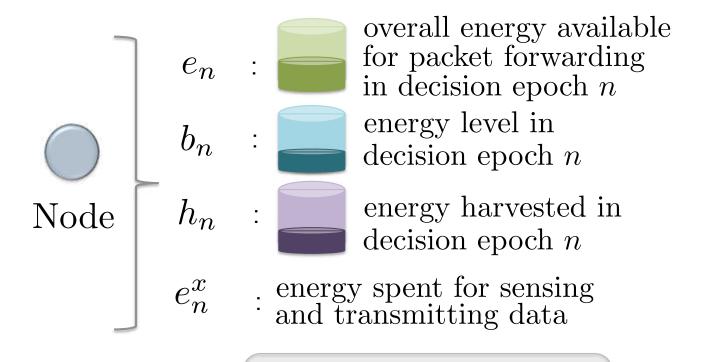


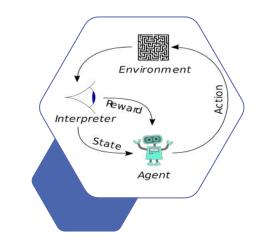
S. Basagni, V. Di Valerio, G. Koutsandria, C. Petrioli, and D. Spenza. "WHARP: A wake-up radio and harvesting-based forwarding strategy for green wireless networks," in *Proceedings of IEEE MASS* 2017, Orlando, FL, USA, October 22–25 2017.

Internet of Things A.Y. 20-21

 $a_n = a_d$

MDP model: States







S. Basagni, V. Di Valerio, G. Koutsandria, C. Petrioli, and D. Spenza. "WHARP: A wake-up radio and harvesting-based forwarding strategy for green wireless networks," in *Proceedings of IEEE MASS* 2017, Orlando, FL, USA, October 22–25 2017.

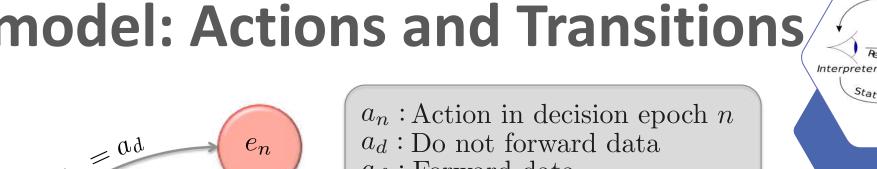
Internet of Things A.Y. 20-21

 $e_n = b_n + h_n - e_n^x$

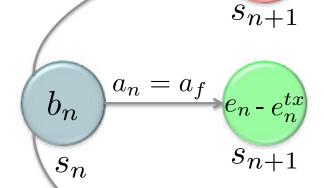
Environment

Agent

MDP model: Actions and Transitions

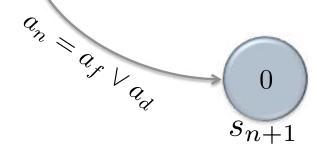


 a_f : Forward data



an

 e_n^{tx} : Energy spent to relay data

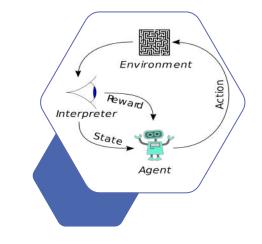


$$s_n = 0 \Rightarrow b_n = 0$$
: All-off node



S. Basagni, V. Di Valerio, G. Koutsandria, C. Petrioli, and D. Spenza. "WHARP: A wake-up radio and harvesting-based forwarding strategy for green wireless networks, "in *Proceedings of IEEE MASS* 2017, Orlando, FL, USA, October 22–25 2017. Internet of Things A.Y. 20-21

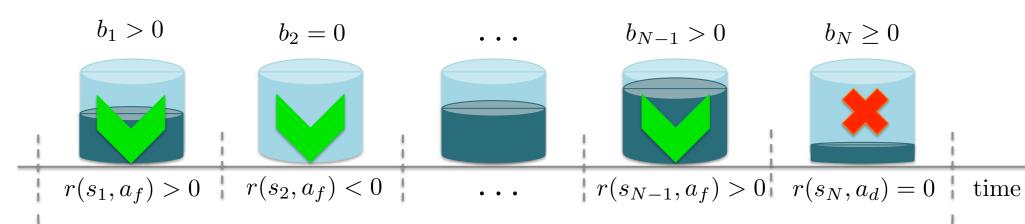
MDP model: Revenue





: action $a_n = a_f$: action $a_n = a_d$





N decision epochs

S. Basagni, V. Di Valerio, G. Koutsandria, C. Petrioli, and D. Spenza. "WHARP: A wake-up radio and harvesting-based forwarding strategy for green wireless networks, "in *Proceedings of IEEE MASS* 2017, Orlando, FL, USA, October 22–25 2017. Internet of Things A.Y. 20-21

WHARP: Performance Evaluation

- Scenario: WHARP vs. EHWA
 - GreenCastalia Simulator
 - M=120; Grid: 200 x 200 m²
 - $R = 60m; R_w = 45m$
 - Energy model: Magonode++ mote

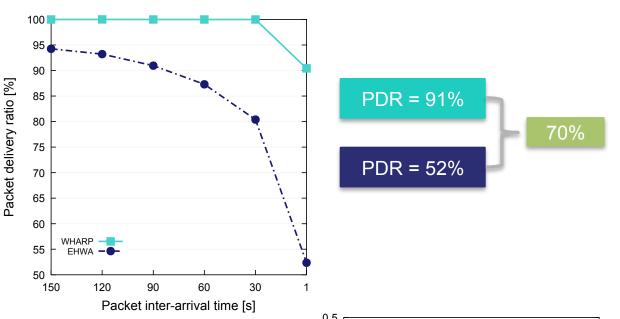


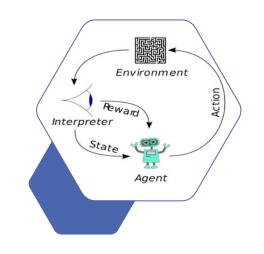




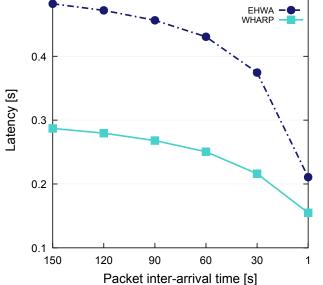
Environment

WHARP: Performance Evaluation



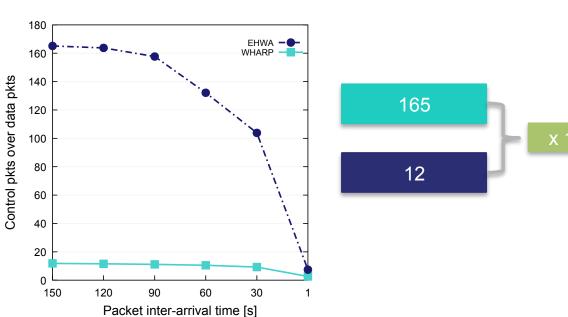


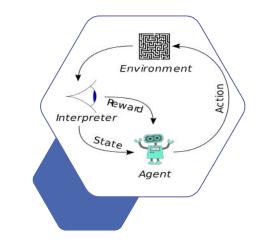




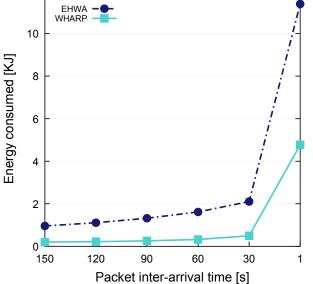


WHARP: Performance Evaluation



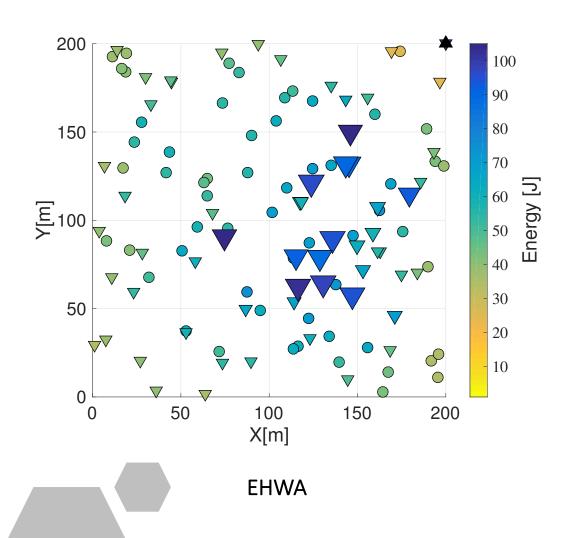


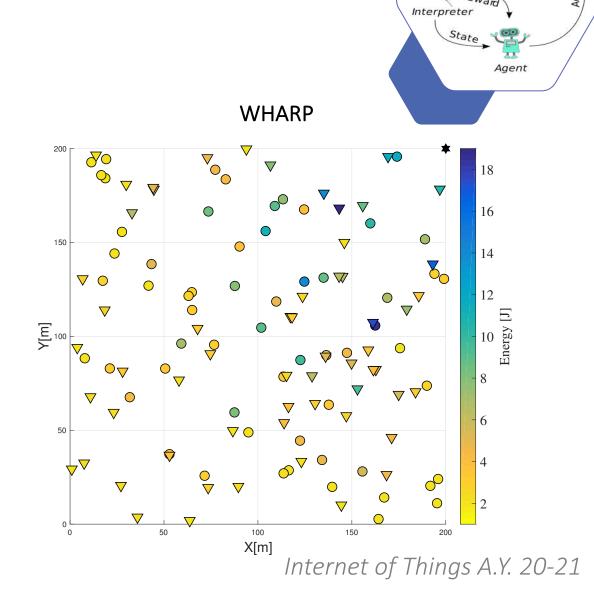




Environment

WHARP: Performance Evaluation





Additional Resources

Environment

Reward

Interpreter

State

Agent

- An Introduction to Reinforcement Learning, Sutton and Barto,
 MIT Press 1998
 - Book available free online:

https://web.stanford.edu/class/psych209/Readings/SuttonBartoIPRLBook2nd Ed.pdf

- Algorithms for Reinforcement Learning, Szepesvari, Morgan and Claypool 2010
 - Book available free online:

https://sites.ualberta.ca/~szepesva/papers/RLAlgsInMDPs-lecture.pdf



