

Advanced Architectures

Prof. A. Massini

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End-of-term test

Student's Name

Matricola number

Exercise 1 (4 points)	
Exercise 2 (4 points)	
Exercise 3 (4 points)	
Question 1 (4 points)	
Question 2 (4 points)	
Exercise 4 (4 points)	
Exercise 5 (4 points)	
Exercise 6 (4 points)	
Total (32 points)	

Exercise 1 (4 points) - GPU & CUDA

You need to write a kernel that operates on a matrix of size **1440x2340**. You would like to assign a thread to each element of the array and use the maximum possible number of threads per block on your device.

a) How would you select the dimensions of a **2D grid** and **2D rectangular blocks** for your kernel, minimizing the number of idle threads? Consider a device having compute capability 1.3.

a) How would you select the dimensions of a **2D grid** and **3D blocks** with the three sides all equal for your kernel, minimizing the number of idle threads? Consider a device having compute capability 3.7.

[illegible]

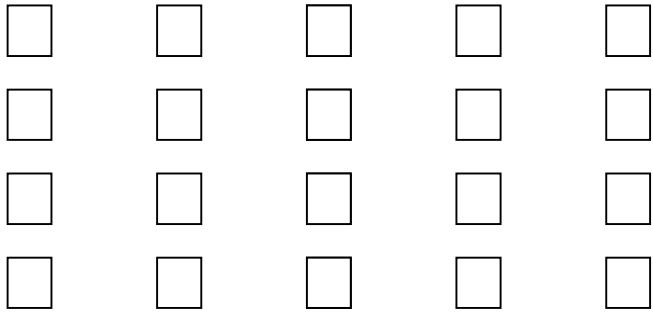
Exercise 2 (4 points) – Interconnection Networks – CLOS

Design a Clos network of size 510×510 , using in the first stage modules having 20 inputs. Consider both cases, strictly non-blocking and rearrangeable network.

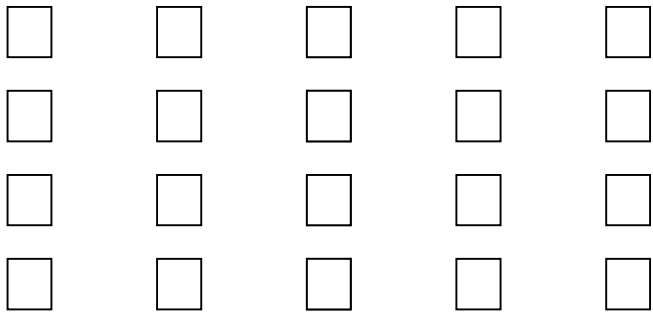
Compare the cost of the crossbar 510×510 and the Clos network, strictly non-blocking and rearrangeable non-blocking, designed in the previous point.

Exercise 3 (4 points) – Interconnection networks – $(2 \log N - 1)$ MIN

Draw a Shuffle-Shuffle network of size $N=8$ using the switches below. Is it possible to realize the permutation $P = \begin{pmatrix} 01 & 23 & 45 & 67 \\ 46 & 10 & 32 & 75 \end{pmatrix}$ setting all the switches in the central stage on the straight state?



Which multistage network with $2 \log N - 1$ stages would you use to route the permutation P above, that guarantees to find a solution? Draw the network and show the connections, making clear how you obtain the final configuration.



Question 1 (4 points)

Briefly explain what entanglement between two qubits is, how it can be explained in mathematical terms and show the expressions of the Bell states.

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Question 2 (4 points)

Explain what CUDA threads are and how they are organized in terms of blocks and grids. Describe how to obtain a unique ID for each thread by using the block ID and thread ID, in the case of a 2D grid and 2D blocks and in the case of 1D grid and 3D blocks.

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Exercises 4 (4 points) – Interconnection networks

Illustrate the design of an XGFT(3; 4, 2, 2; 1, 4, 2), specifying how many nodes there are on each level, how many parents and children they have, and then showing the drawing of the network.

Exercises 5 (4 points) – Quantum qubit systems

a) Verify which of the following systems consisting of two qubits is valid:

$$\psi_1 = \frac{1}{2\sqrt{3}} |00\rangle + \frac{3}{2\sqrt{15}} i |01\rangle + \frac{1}{3} i |01\rangle - \frac{\sqrt{3}}{\sqrt{15}} |11\rangle$$

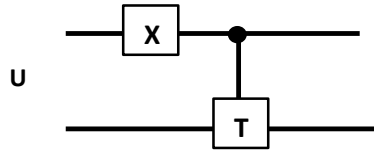
$$\psi_2 = \frac{\sqrt{6}}{6} |00\rangle + \frac{\sqrt{6}}{2\sqrt{3}} i |01\rangle + \frac{1}{2\sqrt{3}} i |01\rangle - \frac{1}{2} |11\rangle$$

b) Compute the probability of measuring $|01\rangle$ for the valid system

c) Compute the two component qubits for the valid system and the probability of measuring $|0\rangle$ for each of them.

Exercise 6 (4 points) – Quantum circuits

Consider the two-qubit transformations U based on gates $X = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$ and $T = \begin{bmatrix} 1 & 0 \\ 0 & e^{i\frac{\pi}{4}} \end{bmatrix}$ shown below



- Show what transformations U represents, writing the associated 4x4 matrices.
- Show how U acts on the state represented by the statevector $\left[\frac{1}{2}; \frac{i}{2\sqrt{3}}; -\frac{i}{\sqrt{2}}; \frac{\sqrt{2}}{2\sqrt{3}}i \right]$.