## Exercise 1:

a) Turn in base 4 the decimal number 243
b) Subtract to the result the number $310_{4}$
c) Turn the resulting number in base 2 and multiply the result by $101_{2}$
d) Turn the result into base 16
e) Consider the number obtained at the end of point (c) as a number in 2-complement and turn it into base 10

Exercise 2: Turn 9,375 10 in IEEE half-precision format. Then, sum it to $<1 ; 10000 ; 1101110000>$, write the result in IEEE half-precision format and finally convert the resulting number in base 10 .

Exercise 3: By using axioms and laws of Boolean algebra, prove the following equlity:

$$
(x \oplus y)(x+\bar{x} y+z)(\bar{y}+\bar{x} y+z)=x \oplus y
$$

Exercise 4: Given the side truth table:
a) Compute y2 by using a 4-to-1 MUX
b) Write a minimal POS for y0
c) Write an ALL-NAND expression for y1
d) Realize the whole function by using a ROM

Exercise 5: Design a combinatorial net for controlling an irrigation system. The system should be open if the time is between 10 pm and 11 pm , and either the weather is sunny or the ground is not wet.

| x 3 x 2 x 1 x 0 | y2 y1 y0 |
| :---: | :---: |
| $\begin{array}{llll}0 & 0 & 0 & \end{array}$ | 0110 |
| $\begin{array}{llll}0 & 0 & 0 & 1\end{array}$ | 110 |
| $\begin{array}{lllll}0 & 0 & 1 & 0\end{array}$ | 110 |
| $\begin{array}{lllll}0 & 0 & 1 & 1\end{array}$ | 110 |
| $\begin{array}{llll}0 & 1 & 0 & 0\end{array}$ | $\begin{array}{llll}0 & 1 & 1\end{array}$ |
| $\begin{array}{llll}0 & 1 & 0 & 1\end{array}$ | $\begin{array}{llll}0 & 1 & 1\end{array}$ |
| $\begin{array}{lllll}0 & 1 & 1 & 0\end{array}$ | $\begin{array}{llll}1 & 1 & 1\end{array}$ |
| $\begin{array}{lllll}0 & 1 & 1 & 1\end{array}$ | 1111 |
| 10000 | 1001 |
| $1 \begin{array}{llll}1 & 0 & 0 & 1\end{array}$ | 1001 |
| $1 \begin{array}{llll}1 & 0 & 1 & 0\end{array}$ | 110 |
| $\begin{array}{llll}1 & 0 & 1 & 1\end{array}$ | $\begin{array}{llll}0 & 1 & 0\end{array}$ |
| 1100 | - - - |
| $\begin{array}{llll}1 & 1 & 0 & 1\end{array}$ | - - - |
| $\begin{array}{llll}1 & 1 & 1 & 0\end{array}$ | 110 |
| $\begin{array}{llll}1 & 1 & 1 & 1\end{array}$ | 110 |

