Name $\qquad$ Surname $\qquad$ Matric.numb. $\qquad$

Exercise 1 ( 3 points): Prove, by using axioms and laws of the Boolean algebra (and by specifying which axiom/law has been used), the following equality:

$$
a b+c(\bar{a}+\bar{b})=a b+c
$$

Exercise 2 (3+1 points): Design a Mealy automaton with input alphabeth $\{\mathrm{X}, \mathrm{Y}, \mathrm{Z}\}$ that accepts the sequences $\mathrm{XXYZ}, \mathrm{XYXY}$ and XYZZ also with overlappings. How would the automaton change if no overlapping was allowed?

Exercise 3 ( 5 points): Design an interconnection net among registers $R_{0}, R_{1}, R_{2}, R_{3}, R_{4}$ and $R_{5}$ such that:

- If the value contained in $R_{0}$ is negative, then the arithmetic sum between $R_{0}$ and $R_{1}$ is moved into $\mathrm{R}_{4}$; otherwise, $\mathrm{R}_{4}$ receives the content of $\mathrm{R}_{3}$;
- If $R_{2}$ is greater than $R_{3}$, then $R_{1}$ is copied into $R_{5}$; otherwise, $R_{5}$ receives $R_{3}$;
- $\quad R_{4}$ is copied into register $R_{i}$ where $i$ is given by the two less signifying bits of $R_{5}$.

The transfers are enabled only when the content of $\mathrm{R}_{0}$ is a negative integer.

Exercise 4 (4 points): Turn into base 8 the number $339_{10}$. Then, sum $267_{8}$ to the obtained number, turn the result in base 2 and calculate the opposite of this number in 2 -complement format with 12 bits.

Exercise 5 ( 3 points): Let $A=<0 ; 01111 ; 0011100000>$ and $B=<1 ; 10001 ; 0011100000>$ be two numbers in the IEEE half-precision format. Sum them and represent the result in the same format.

Exercise 6 (3+2 points): Consider the following automaton with initial state SO:

|  | 0 | 1 |
| :--- | :--- | :--- |
| S0 | S1/1 | S0/0 |
| S1 | S2/0 | S3/1 |
| S2 | S1/0 | S4/1 |
| S3 | S1/0 | S0/0 |
| S4 | S2/0 | S0/0 |
| S5 | S2/0 | S3/0 |

Minimize it and then provide (for the minimal automaton) the temporal diagram for the input 000101.

Exercise $\mathbf{7 ( 2 + 2 + 2}$ points): Consider the following combinatorial circuit:

a) Write the boolean expression associated to $y$ and its truth table;
b) Find a minimal SOP for $y$;
c) Turn the resulting expression in ALL-NAND form.

