## Advanced and parallel architectures

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June 13, 2017

## Part B

Student's Name

## Matricola number

| Exercise 1a (3 points) |  |
| :--- | :--- |
| Exercise 1b (3 points) |  |
| Exercise 2 (8 points) |  |
| Exercise 3 (4 points) |  |
| Exercise 4 (3 points) |  |
| Exercise 5 (3points) |  |
| Exercise 6 (4 points) |  |
| Exercise 7 (4 points) |  |
| Total (32 points) |  |

## Exercise 1a (3 points) - Interconnection Networks - CLOS

Design a Clos network of size $150 \times 150$, using in the first stage modules having 24 inputs. Consider both cases, strictly non-blocking and rearrangeable network.

## Exercise 1b (3 points) - Interconnection Networks - Comparison Clos-Crossbar

Compare the cost of the crossbar $150 \times 150$ and the Clos network, strictly non-blocking and rearrangeable, designed in the previous point.

## Exercise $\mathbf{2}$ (4+2+2 points) - GPU \& CUDA

You need to write a kernel that operates on a 2D matrix of size $15000 \times 4500$. You would like to assign one thread to each matrix element. You would like your thread blocks to use the maximum number of threads per block possible on your device, having compute capability 3.0.
a) How would you select the dimensions of a 2D grid and 2D blocks for your kernel? Consider the two cases of rectangular and square blocks
b) How would you select the dimensions of a 3D grid and 2D blocks for your kernel?
c) What is the best choice for grid and block dimensions with respect to the number of idle threads?

| Technical specifications | Compute capability (version) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1.0 | 1.1 | 1.2 | 1.3 | 2.x | 3.0 | 3.5 | 3.7 | 5.0 | 5.2 |
| Maximum dimensionality of grid of thread blocks | 2 |  |  |  | 3 |  |  |  |  |  |
| Maximum x-dimension of a grid of thread blocks | 65535 |  |  |  |  | $2^{31}-1$ |  |  |  |  |
| Maximum y -, or z -dimension of a grid of thread blocks | 65535 |  |  |  |  |  |  |  |  |  |
| Maximum dimensionality of thread block | 3 |  |  |  |  |  |  |  |  |  |
| Maximum x- or y-dimension of a block | 512 |  |  |  | 1024 |  |  |  |  |  |
| Maximum z-dimension of a block | 64 |  |  |  |  |  |  |  |  |  |
| Maximum number of threads per block | 512 |  |  |  | 1024 |  |  |  |  |  |
| Warp size | 32 |  |  |  |  |  |  |  |  |  |
| Maximum number of resident blocks per multiprocessor | 8 |  |  |  |  |  | 16 |  |  |  |
| Maximum number of resident warps per multiprocessor | 24 |  | 32 |  | 48 | 64 |  |  |  |  |
| Maximum number of resident threads per multiprocessor | 768 |  | 1024 |  | 1536 | 2048 |  |  |  |  |
| Technical specifications | 1.0 | 1.1 | 1.2 | 1.3 | 2.x | 3.0 | 3.5 | 3.7 | 5.0 | 5.2 |
|  | Compute capability (version) |  |  |  |  |  |  |  |  |  |

## Exercise 3 (4 points) - Cache coherence

Consider a multicore multiprocessor implemented as a symmetric shared-memory architecture, as illustrated in the figure.
Each processor has a single, private cache with coherence maintained using the snooping coherence protocol. Each cache is direct-mapped, with four blocks each holding two words. The coherence states are denoted M, S, and I (Modified, Shared, and Invalid).

Each part of this exercise specifies a sequence of one or more CPU operations of the form:

P\#: <op> <address> [<value>]
where P\# designates the CPU (e.g., PO ), <op> is the CPU operation (e.g., read or write), <address> denotes the memory address, and <value> indicates the new word to be assigned on a write operation.

For each part of this exercise, assume the initial cache and memory state as illustrated in the figure.

Show in the table for the results:

- miss/hit
- the coherence state before the action
- the CPU processor Pi and cache block Bj
- the changed state (i.e., coherence state, tags, and data) of the caches and memory after the given action.

| P0 |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Coherency <br> state | Address <br> tag | Data |  |  |  |  |  |  |  |
| B0 | M | 116 | 00 | 28 |  |  |  |  |  |  |
| B1 | M | 120 | 00 | 32 |  |  |  |  |  |  |
| B2 | I | 108 | 00 | 12 |  |  |  |  |  |  |
| B3 | S | 112 | 00 | 32 |  |  |  |  |  |  |


| P1 <br> State |  |  |  |  |  | Address <br> tag | Data |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B0 | I | 116 | 00 | 08 |  |  |  |  |
| B1 | I | 104 | 00 | 08 |  |  |  |  |
| B2 | S | 108 | 00 | 20 |  |  |  |  |
| B3 | S | 112 | 00 | 32 |  |  |  |  |
|  |  |  |  |  |  |  |  |  |


| P2 | Coherency <br> state | Address <br> tag | Data |  |
| :---: | :---: | :---: | :---: | :---: |
| B0 | M | 100 | 00 | 16 |
| B1 | I | 120 | 00 | 28 |
| B2 | S | 108 | 00 | 20 |
| B3 | I | 128 | 00 | 16 |
|  |  |  |  |  |


| P3 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Coherency <br> state | Address <br> tag | Data |  |
| B0 | I | 100 | 00 | 12 |
| B1 | M | 104 | 00 | 28 |
| B2 | S | 108 | 00 | 20 |
| B3 | M | 128 | 00 | 12 |



Specify the value returned by a read operation.

| hit/miss | state <br> before | Pi.Bj (state, tag, datawords) |
| :--- | :--- | :--- |
|  |  |  |
|  |  |  |
|  |  |  |

b) P1: write $124 \leftarrow 24$

| hit/miss | state <br> before | Pi.Bj (state, tag, datawords) |
| :--- | :--- | :--- |
|  |  |  |
|  |  |  |
|  |  |  |

c) P3: read 120

| hit/miss | state <br> before | Pi.Bj (state, tag, datawords) |
| :--- | :---: | :--- |
|  |  |  |
|  |  |  |
|  |  |  |

d) PO: write $100 \leftarrow 32$

| hit/miss | state <br> before | Pi.Bj (state, tag, datawords) |
| :--- | :---: | :--- |
|  |  |  |
|  |  |  |
|  |  |  |

## Exercise 4 (3 points) - Interconnection networks - $\log$ N MIN

Complete the scheme Baseline networks of size $N=8$. Show if it can realize the permutation $P=\binom{01234567}{40367152}$ showing the switch setting obtained using the self-routing.


## Exercise 5 (3 points) - Interconnection networks - ( $2 \log \mathbf{N}-1$ ) MIN

Complete the scheme of the Butterfly-Butterfly ${ }^{-1}$. Show the switch setting to realize permutation $P=\binom{01234567}{40367152}$ according to the looping algorithm.


## Exercises 6 (4 points) Amdhal Law

The following measurements are recorded with respect to the different instruction classes for the instruction set running a given set of benchmark programs:

| Instruction Type | Instruction Count (millions) | Cycles per Instruction |
| :--- | :---: | :---: |
| Arithmetic and logic | 6 | 4 |
| Load and store | 8 | 2 |
| Branch | 4 | 4 |
| Others | 6 | 4 |

Assume that "Arithmetic and logic" instructions can be modified so that they take 3 cycles per instruction instead of 4, and "Branch" instructions can be modified so that they take 2 cycle per instruction instead of 4 as in the table. Compute the speedup obtained by introducing only one enhancement and both enhancements using the Amdhal law.

## Exercises 7 (4 points) Performance equation

Suppose we have made the following measurements, where we are considering Arithmetic instructions and FP (Floating Point):
Frequency of Arithmetic operations $=35 \%$
Average CPI of Arithmetic operations $=4.0$
Average CPI of other instructions $=2.5$
Frequency of FP operations $=15 \%$
CPI of $\mathrm{FP}=8.0$
Assume that the two design alternatives are to decrease the CPI of FP to 3.0 or to decrease the average CPI of Arithmetic operations to 2.5.
Compare these two design alternatives using the processor performance equation, and compute the speedup in both cases.

